
WHAT IS CFD?

1.1 INTRODUCTION

We start with a definition

CFD (Computational Fluid Dynamics) is a set of numerical methods applied to obtain approximate solutions of problems of fluid dynamics and heat transfer.

According to this definition, CFD is not a science on its own but a way to apply the methods of one discipline (numerical analysis) to another (heat and mass transfer). We will deal with details later. Right now, a brief discussion is in order of why exactly we need CFD.

A distinctive feature of the science of fluid flow and heat and mass transfer is the approach it takes toward description of physical processes. Instead of bulk properties, such as momentum or angular momentum of a body in mechanics or total energy or entropy of a system in thermodynamics, the analysis focuses on *distributed properties*. We try to determine the entire

fields such as temperature $T(\mathbf{x}, t)$, velocity $\mathbf{v}(\mathbf{x}, t)$, density $\rho(\mathbf{x}, t)$, etc.¹ Even when an integral characteristic, such as the friction coefficient or the net rate of heat transfer, is the ultimate goal of the analysis, it is derived from distributed fields.

The approach is very attractive by virtue of the level of details it provides. Evolution of the entire temperature distribution within a body can be determined. The effect of internal processes of a fluid flow such as motion, rotation, and deformation of minuscule fluid particles can be taken into account. Of course, the opportunities come at a price, most notably in the form of dramatically increased complexity of the governing equations. Except for a few strongly simplified models, the equations for distributed properties are *partial differential equations*, often nonlinear.

As an example of complexity, let us consider a seemingly simple task of mixing and dissolving sugar in a cup of hot coffee. An innocent question of how long would it take to completely dissolve the sugar leads to a very complex physical problem that includes a possibly turbulent two-phase (coffee and sugar particles) flow with variable physical properties and a chemical reaction (dissolving). Heat transfer (within the cup and between the cup and surroundings) is also of importance because temperature strongly affects the rate of the reaction. No simple solution of the problem exists. Of course, we can rely on the experience acquired after repeating the process daily (perhaps more than once) for many years. We can also add a couple of extra, possibly unnecessary, stirs. If, however, the task in question is more serious – for example, optimizing an oil refinery or designing a new aircraft – relying on everyday experience or excessive effort is not an option. We must find a way to *understand* and *predict* the process.

Generally, we can distinguish between three approaches to solving fluid flow and heat transfer problems:

1. *Theoretical approach*: Finding analytical solutions of governing equations or arriving to conclusions on the basis of some theoretical considerations.
2. *Experimental approach*: Staging an experiment using a model of the real object.
3. *Numerical approach*: Using computational procedures to find a solution of the governing equations.

¹Throughout the book, we will use $\mathbf{x} = (x, y, z)$ or $\mathbf{x} = (x_1, x_2, x_3)$ for the vector of space coordinates and t for time.

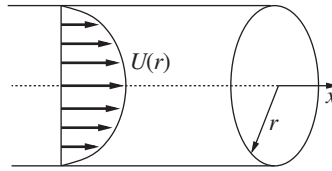


Figure 1.1 Laminar flow in an infinite pipe.

Let us look at these approaches in more detail.

Theoretical Approach. The approach has a crucial advantage of providing exact solutions. Among the disadvantages, the most important is that analytical solutions are only possible for a very limited class of problems, typically formulated in an artificial, idealized way. One example is the Hagen–Poiseuille solution for a flow in an infinitely long pipe (see Figure 1.1). The steady-state laminar velocity profile is

$$U(r) = \frac{r^2 - R^2}{4\mu} \frac{dp}{dx},$$

where U is the velocity, R is the pipe radius, dp/dx is the constant pressure gradient that drives the flow, and μ is the dynamic viscosity of the fluid. The solution is, indeed, simple and gives insight into the nature of flows in pipes and ducts, so its inclusion into all textbooks of fluid dynamics is not surprising. At the same time, the solution is correct only if the pipe is infinitely long,² temperature is constant, and the fluid is perfectly incompressible. Furthermore, even if we were able to build such a pipe and find some use for it, the solution would be correct only at Reynolds numbers $Re = UR\rho/\mu$ (ρ is the density of the fluid) below, approximately, 1200. Above this limit, the flow would take fully three-dimensional and time-dependent transitional or turbulent form, for which no analytical solution is possible.

It can also be noted that derivation of analytical solutions often requires substantial mathematical skills, which are not among the strongest traits of many modern engineers and scientists, especially if compared to the situation of 30 or 40 years ago. Several reasons can be named for the deterioration of such skills, one, no doubts, being development of computers and numerical methods, including the CFD.

²In practice, the solution is considered to be a good approximation for laminar flows in pipes at sufficiently large distance (dependent on the Reynolds number but at least few tens of diameters) from the entrance.

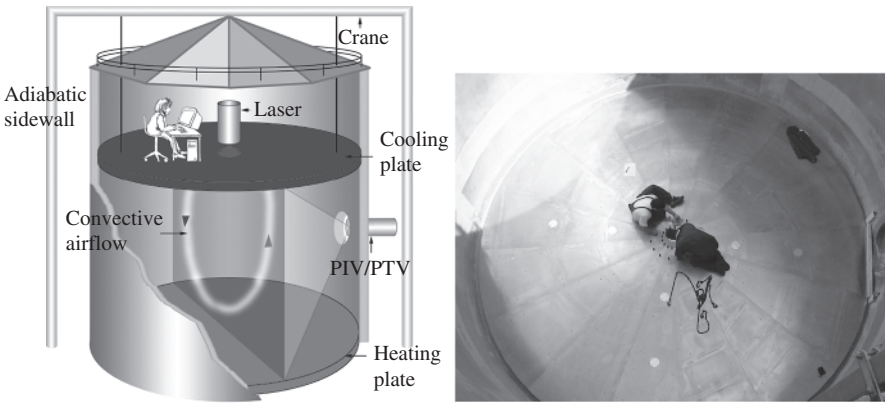


Figure 1.2 The experiment for studying thermal convection at the Ilmenau University of Technology, Germany. Turbulent convection similar to the convection observed in the atmosphere of Earth or Sun is simulated by air motion within a large barrel with thermally insulated walls and uniformly heated bottom. Source: Courtesy of André Thess.

Experimental approach: Well-known examples are the wind tunnel experiments, which help to design and optimize the external shapes of air-planes (also of ships, cars, buildings, and other objects). Another example is illustrated in Figure 1.2. The main disadvantages of the experimental approach are the technical difficulty (sometimes it takes several years before an experiment is set up and all technical problems are resolved) and high cost.

Numerical (computational) approach: Here, again, we employ our ability to describe almost any fluid flow or heat transfer process as a solution of a set of partial differential equations. An approximation to this solution is found by a computer executing an algorithm. This approach is not problem-free either. We will discuss the problems throughout the book. The computational approach, however, beats the analytical and experimental methods in some very important aspects: universality, flexibility, accuracy, and cost.

1.2 BRIEF HISTORY OF CFD

The history of CFD is a fascinating subject, which, unfortunately, we can only touch in passing. The idea to calculate approximate solutions of differential equations describing fluid flows and heat transfer is relatively old, definitely older than computers themselves. Development of numerical

methods for solving ordinary and partial differential equations started in the first half of the twentieth century. The computations at that time required the use of calculation tables and dull mechanical work of tens, if not hundreds, of people. No wonder that only the apparently most important (often military-related) problems were addressed and only simple one-dimensional equations were solved.

Invention and subsequent fast development of computers opened a wonderful possibility of performing millions and, then, millions of millions of arithmetic operations in a matter of seconds. Together with the rapid development of the algorithms of numerical mathematics, this has led to impressive growth of speed and abilities of CFD analysis. First simulations of realistic two-dimensional flows were performed in the late 1960s, while three-dimensional flows could be seriously approached since the 1980s. Again, military tasks, such as modeling shock waves from an explosion or a flow past a hypersonic jet aircraft, were addressed first. In fact, development of faster and bigger computers until 1980s was largely motivated by the demands of the military-related CFD.

Over the last several decades, the field of CFD has changed profoundly. From a scientific discipline, in which researchers worked on unique projects using specially developed codes, it has transformed into *an everyday tool of engineering design and scientific research*. In engineering, the simulations are routinely used as “virtual experiments” replacing or complementing prototyping and other design techniques. The problem-specific codes are still developed for scientific purposes, but the practice has almost entirely switched to the use of commercial or open-source CFD codes. The market is largely divided between few major brands, such as ANSYS, STAR-CCM, OpenFOAM, or COMSOL. Standard codes are widely used in other areas of active CFD applications, such as meteorology, oceanography, or astrophysics. The codes differ in appearance and capabilities but are all essentially numerical solvers of partial differential equations with attached physical and turbulence models and algorithms for grid generation and post-processing of results.

1.3 OUTLINE OF THE BOOK

This book is intended as a brief but complete introduction into CFD. The focus is not on development of algorithms but on the fundamental principles, formulation of CFD problems, the most basic and common computational techniques, and essentials of a good CFD analysis. The book’s main task is

to prepare the reader to make educated choices while using one of the available CFD codes. A reader seeking deeper and more detailed understanding of specific computational methods is encouraged to use more advanced and more specialized texts, references to some of which are presented at the end of each chapter.

A comment is in order regarding the bias of the text. All CFD texts are, to some degree, biased in correspondence with the chosen audience and personal research interests of the authors. More weight is given to some of the methods (finite difference, finite element, spectral, etc.) and some of the fields of application (heat transfer, incompressible fluid dynamics, or gas dynamics). The preferences made in this book reflect the choice of mechanical, chemical, biomedical, and civil engineers as the target audience and the intended use for applied CFD instruction. The focus is on the finite difference and finite volume methods. The finite element and spectral techniques are introduced, but only briefly. Also, more attention is given to numerical methods for incompressible fluid dynamics and heat transfer than for compressible sub- and supersonic flows.

The book contains 13 chapters. We are already at the end of Chapter 1. The remaining chapters are separated into three parts: “Fundamentals,” “Methods,” and “Art of CFD.” Part I deals with the basic concepts of numerical solution of partial differential equations. It starts with Chapter 2 introducing the equations we are most likely to solve: the governing equations of fluid flows and heat transfer. We consider various forms of the equations used in CFD and review common boundary conditions. Necessary mathematical background and the concept of numerical approximation are presented in Chapter 3. Chapter 4 discusses the basics of the finite difference method. We also introduce the key concepts associated with all CFD methods, such as the truncation error and consistency of numerical approximation. The principles and main tools of the finite volume method are presented in Chapter 5. Chapter 6 is devoted to the concept of stability of numerical time integration. Some popular and important (both historically and didactically) schemes for one-dimensional model equations are presented in Chapter 7. This material summarizes the discussion of the fundamental concepts and can be used for a midterm programming project.

Part II, which includes Chapters 8–10, contains a compact description of some of the most important and commonly used CFD techniques. Methods of solution of systems of algebraic equations appearing in the result of the CFD approximation are discussed in Chapter 8. Chapter 9 presents some schemes used for unsteady heat conduction and compressible flows. The discussion is deliberately brief for such voluminous subjects. It is expected

that a reader with particular interest in any of them will refer to other, more specialized, texts. Significantly more attention is given to the methods developed for computation of flows of incompressible fluids. Chapter 10 provides a relatively broad explanation of the issues, presents the projection method, and introduces some popular algorithms.

Part III consists of Chapters 11–13 and deals with subjects that are not directly related to the numerical solution of partial differential equations, but nevertheless are irreplaceable in practical CFD analysis. They all belong to a somewhat imprecise science in the sense that the approach is often decided on the basis of knowledge and experience rather than exact knowledge alone. The subjects in question are the turbulence modeling (Chapter 11), design and quality of computational grids (Chapter 12), and the questions arising in the course of CFD analysis, such as uncertainty and validation of results (Chapter 13). The discussion is, by necessity, brief. A reader willing to acquire truly adequate understanding of these difficult but fascinating topics should consult the books listed at the end of each chapter.

BIBLIOGRAPHY

A rich source of information on CFD, online since 1994: books, links, discussion forums, jobs, etc. <http://www.cfd-online.com/>.

Official web site of the TOP500 project providing reliable and detailed information on the world most powerful supercomputers. <http://www.top500.org/>.

